**Interim Report**

**November 2016**

**Word count = 3080**

**Abstract**

**1. Introduction**

N-body simulations of physical systems are a key factor to solving and understanding problems in science, they can be used to help the understanding of interactions between molecules and to help visualize the Brownian motion in molecular dynamics and are widely used in astrophysics. Astrophysical simulations are used to help predict the effects of dark matter on astronomical bodies, and can also help to understand and theorize the theoretical models of phenomena’s such as star formation.

**1.1 Star formation**

Perturbations such as shock waves from nearby supernovae and collisions between two giant molecular clouds (GMC) can lead to contractions on the clouds, if the contraction of these clouds surpasses a certain radius called the Jeans radius, gravity overcomes turbulences and thermal pressure and becomes the dominant force and produces a dynamical collapse which is uncontrollable. This is process sparks the beginning of star formation. (Appenzeller, et al., 1980)

During this collapsing phase of the molecular cloud, the original molecular cloud breaks up into smaller clouds through fragmentation. This collapsing process increases the opacity of the clouds and leads to an increase in temperature and therefore using the ideal gas laws the pressure built up inside the clouds increases. The fragmentation process is halted when hydrostatic equilibrium is reached, this results in the formation of a protostar.

An envelope of gas and dust surrounds the protostar which due to gravity accretes onto the protostar which increases the mass and temperature of the protostar, the lack of an envelope leads to a pre-main-sequence star (PMS star). A PMS star is a star that has yet to start hydrogen burning through nuclear fusion. Once the protostar’s opacity increases to the point that the gravitational contraction causes the temperature to increase to a point that hydrogen burning can start, the star is then said to be a main-sequence star (MS star). This is a generally accepted overview of star formation.

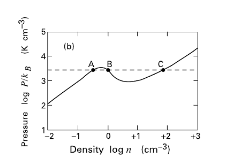
**1.2 Main stages of star formation**

To delve deeper into the details of star formation requires a combination of accepted and disputed peer reviewed papers. This section will go deeper into star formation by discussing each of the main stages of star formation.

**1.2.1 Giant molecular clouds and the Interstellar medium**

The interstellar medium (ISM) is defined as the “stuff” that occupies the space between stars. This “stuff” is predominantly made up of matter and electromagnetic radiation. The ISM can be split up into five different thermal phases (Ryden & Pogge, 2016). The first phase is the hot ionized medium (HIM); this phase occupies of the ISM, in it includes low density gas that is heated up to temperatures of over K due to supernovas, powerful winds from the largest progenitor stars and UV radiation, the gas in the HIM can be detected by X-ray emission and absorption lines in the UV region of the spectrum.

The second phase is the warm ionized medium (WIM); Using results provided by Ferrière (2001), it is thought that this phase occupies of the ISM and is made up of ionized hydrogen atoms (H+ or HⅡ). It is thought that most HII arises from the photoionization with strong UV radiation from O and B stars, which creates regions of HII around most O and B stars. The temperatures of the WIM range between 6000 to 10,000 K and is regulated by the heating of the photoionization of the hydrogen atoms and the cooling from Lyman alpha line emission (Lyα). The gas in the WIM can be traced using the Hα emission observed at a wavelength of 656.3nm.

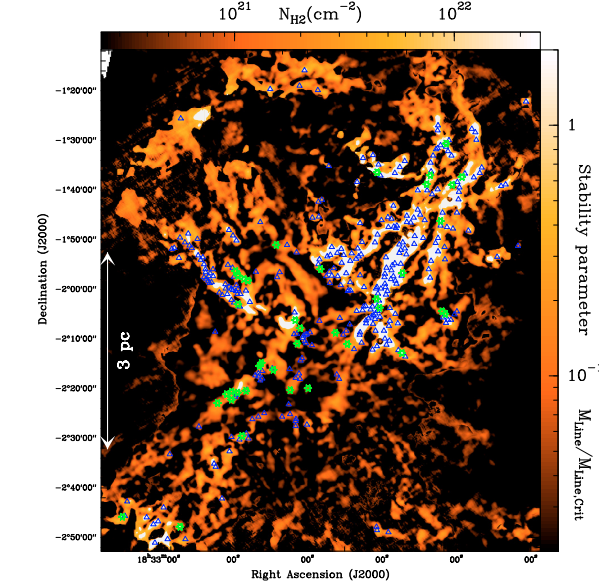
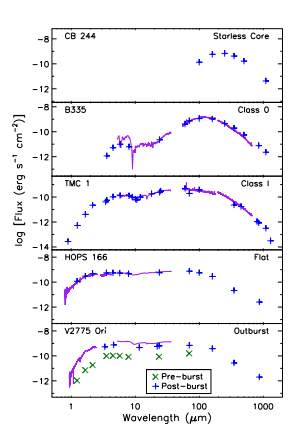


**Figure 1** Theoretical prediction of equilibrium pressure as a function of number density. (Wolfire, et al., 1995)

The third and four phases are the warm neutral medium (WNM) and cold neutral medium (CNM); both phases together occupy of the ISM and have number densities of and cm-3 for the WNM and CNM respectively, it is mostly made up of neutral hydrogen (HI) and is heated to K in the WNM and K in the CNM. Both phases are heated by various ways; such as photoelectrons ejected from dust grains and cosmic rays ionizing atoms through collisions. It was first suggested by Field, et al. (1969) that the two phases are in thermal pressure equilibrium since , where n is the density and T is the temperature. This agrees with the theoretical prediction for the equilibrium pressure as a function of density (as seen in Figure 1), where the WNM matches the stable point A and the CNM matches the stable point C, the point B represents an unstable point at which a perturbation causes the gas to fall into one of the stable points depending on the conditions of the perturbation. The CNM is cooled through the de-excitations of collisionally excited fine-structure lines of C+ and other metals. The CNMcan be traced using the C+emission line observed at a wavelength of 158μm (Bennett, et al., 1994). The WNM on the other hand has a very similar cooling mechanism to the WIM, where the Lyα emission is again the main cooling mechanism. The WNM can be traced using the 21cm emission line of HI formed due the spin-flip transition between two hyperfine energy levels, which was first discovered by Ewen & Purcell (1951). [Do I need these first three phases in detail?]

The final phase is the molecular cloud; this phase is cold enough to give rise to interstellar molecular gas such as CN and CH (Swings & Rosenfeld, 1937), and were found through absorption lines produced in stellar spectra. The temperatures inside molecular clouds range between – K with densities of over 103 cm-3 and occupy of the ISM. Although the molecular clouds only occupy a very small percentage of the ISM, the contribution of the fractional ISM mass from molecular clouds is much greater than the volume of the ISM it occupies, due to the much heavier elements that are present in the molecular clouds compared to the other phases. The most abundant molecules in the molecular clouds are molecular hydrogen (H2)and carbon monoxide (CO). Relative to the overall number of hydrogen nuclei, the abundance of H2 is given by and the abundance of COis given by (Clark, et al., 2012). Carbon monoxide arises in molecular clouds through a series of reactions between C+, H2 and neutral oxygen (OI). Although molecular hydrogen is the most abundant molecule in these molecular clouds, it is in fact the CO that is main cooling mechanism in the molecular clouds. It is suggested by Glover & Clark (2012) that H2 provides a particularly inefficient cooling, due to widely spaced energy levels of ~ 170 J K, it is therefore particularly difficult to excite molecular hydrogen at low temperatures [contrasting to old theories]. The temperatures of the molecular cloud can reach as low as 10 K due to the rotational excitation of CO which has very low energy levels compared to that of hydrogen, and therefore can be exited at lower temperatures, resulting in cooling through the emitted photons that have been released from the rotational transition. The emission line of CO is the primary tracer of molecular clouds due to the high abundance of CO in molecular clouds. The C+ fine structure excitation also plays a key role in cooling the molecular cloud, it was shown by Glover & Mac Low (2007) that C+ could cool the molecular gas down to ~20 K and was also suggested by Glover & Clark (2012) that molecular gas wasn’t necessary due to C+ cooling, however this is still heavily debated throughout the scientific community. Observations of these molecular clouds are often very difficult to obvserve due to the obscuration of starlight from interstellar dust as a result of absorption and scattering. Dust grains are solid materials composed mainly of carbon, silicon and oxygen and vary in size from a few microns down to the size of a few atoms (Draine, 2003). Dust provides another way of keeping the molecular clouds cool, through gas-grain collisions, the excited gas can release their energy to the dust grains in the form of collisions, which is then re-radiated away. When a molecular cloud contracts it behaves isothermally due to the mean free path of the photons realesed being very large and can be freely radiated away from the cloud (Ward-Thompson & Whitworth, 2011).

The largest of these molecular clouds are called Giant molecular clouds (GMC). Typically, they have masses greater than with similar properties to that of molecular clouds. It is generally agreed that most stars form within the GMC [reference] through external forces acting on GMCs and through turbulences. Turbulences can be described as an unstable flow of gas and are still a highly debated topic due to the very complicated physics involved. Usually the GMC will not have a uniform density throughout, instead most will have locally dense regions and tend to have a dense core. These cores are usually called ‘starless cores’ or ‘pre-stellar cores’ dependant on whether the core is gravitationally bound or not.



**Figure 2** A column density map of Aquila derived from the SPIRE data. The candidate Class 0 protostars and bound prestellar cores identified in Aquila by Bontemps, et al. (2010) and Könyves, et al. (2010) are shown as green stars and blue triangles. (André, et al., 2010)

**Figure 3** An example of SEDs for a starless core, a Class 0 protostar, a Class 1 protostar, a Flat-SED source and an outbursting Class 1 protostar. (Dunham, et al., 2014)

**1.2.2 Filamentary structures and pre-stellar cores**

Filamentary structures have been a renewed topic of interest thanks to the recent Gould Belt Survey, one of the key projects with *Herschel*. Filamentary structures are thin, elongated features with some of the highest colum densities observed in molecular clouds. Filaments were known long before *Herschel,* dating back to at least 1979 where Schneider & Elmegreen (1979) documented dark globular filaments. Arzoumanian, et al. (2013) suggest that filaments form through turbulences in the MCs, although further observations are needed to further our understanding of the formation of filaments. Evidence from *Herschel* suggests that prestellar cores result from the fragmentation of the filaments, and can be seen in Figure 2 (André, et al., 2010). [needs work]

­­A pre-stellar core is defined as a dense core in a molecular cloud that is gravitationally bound and that will collapse into a star as they’re self-gravitating. Pre-stellar cores are observed at far-infrared wavelengths, indicating that these cores are very cold (Ward-Thompson, et al., 2002). These pre-stellar cores can be characterized by looking at the spectral energy distribution (SED) as seen in Figure 3.

Stars form when pre-stellar cores become gravitationally unstable and begin to collapse, this occurs when gravity overcomes pressure, rotation, turbulence and magnetic fields. Assuming a spherical cloud of uniform density, a simple derivation can be made to find the distance at which the core collapses through equating the centripetal force with the gravitational force of the molecular cloud, this is called the Jeans length. This is stated as,

where is called the Jeans length, is the isothermal sound speed, G is the gravitational constant and is the initial uniform density. We can also find the minimum mass associated with the Jeans length, which is stated as,

where is the Jeans mass. This is the minimum mass at which the core starts to collapse due to its own self-gravity. Therefore, the mass of the cloud must be greater than the Jeans mass in order for the core to collapse. We state a dependency of the Jeans mass with the temperature of the cloud through equating the internal energy of the cloud and its kinetic energy,

where T is the temperature of the cloud. Therefore, if the temperature was to increase the Jeans mass would also increase. To understand the duration of the core collapse, we can derive a timescale using crude assumptions, which include the core collapsing freely and isothermally, [check]

where is the free-fall timescale. The collapse of a core is roughly an order of magnitude larger than the free-fall timescale due to the influence of the magnetic field and turbulences, which suggests that the cores are not in free-fall collapse (Ward-Thompson & Whitworth, 2011; Ward-Thompson & Jessop, 1996).

* + 1. **Fragmentation and Protostars**

It was previously thought that parts of the cloud break up into smaller fragments during a collapse through hierarchical fragmentation, since the density of the cloud increases during the contraction, the Jeans mass decreases and parts of the original cloud become gravitationally unstable and start to contract on themselves leading to fragmentation. This process was thought to be based on a homologous collapse (Hunter, 1964), but due to the recent survey, it is now proposed that filaments fragment into prestellar cores when areas of the filaments surpass the Jeans mass, these cores then undergo further fragmentation (André, et al., 2010). During the collapse phase of a prestellar core, the prestellar core is thought to fragment into smaller cores which collapse and form protostars (André, et al., 2009). The opacity in protostars are at a point where photons can not be freely radiated away, which causes an increase in its temperature and due to equation 3 the Jeans mass increases and the protostar eventually becomes gravitationally stable. These protostars are buried deep inside a gaseous envelope with a surrounding circumstellar disk that is produced due to the angular momentum of the protostar, and can only be observed through outflow presence. At this stage in time protostars can be classified as Class 0 objects that can be inferred via the SED as seen in Figure 3 (Andre, et al., 1993; Dunham, et al., 2014). The protostar remains cool due to the low opacity, and the mean free path of photons remain, and also due to cooling from colliding dust grains. The surrounding envelope accretes onto the protostar through Bondi accretion, assuming a spherically symmetric accretion Bondi accretion is where the protostar accretes matter through gravity and traces a cylinder through the envelope due to the differences in the relative motion of the envelope and the protostar andaccretes matter as its moving through the envelope. The protostar can be classed as a Class 1 object at this point and can be characterized by its SED as seen in Figure 3. The protostar is said to be a Class 2 object once the surrounded envelope has been accreted onto the protostar and can be inferred via the SED as seen in Figure 3. [struggling here]

* + - * [protoplanetary disks]
* Binary stars and multiplicity.
* IMF and the class system
* Elliptical orbit

**2. Outline**

Due to the recent findings of the Gould Belt Survey, filamentary structures have received recent special interest and have now surpassed the older theories of a spherical collapse. Our project intends to rectify some of the research made on protostars that assumed spherical collapse, through researching protostars inside filamentary structures. Our goal is to create initial conditions that represent our current understanding of how protostars behave inside these filamentary structures by modelling a N-body simulation of these protostars inside filaments. One of many possible outcome from our simulation could lead to ejecta’s of protostars from these filaments, formation of binary stars and the eccentricity of protostellar orbits, our project will try to achieve these possible results from our initial conditions.

To model the orbital path of the protostars, we use a modified version of Newtons law of Gravity which was originally formalized by Sverre Aarseth, who created the NBODY codes. We use the NBODY2 code which states that,

where is the gravitational acceleration on a protostar of index i, G is the gravitational constant, the j notation is for all the other particles with mass and coordinates and finally the softening parameter is defined as . The introduction of a softening parameter prevents a singularity as the separation of tends to zero (Aarseth, 2001). Using the acceleration of the particles, the orbits can be found through numerical integration using a computer programming language, usually C, C++ or Fortran. The Verlet method was the most suitable method of integration for us due to its simplicity and its higher order accuracy over the Euler method, which can be stated as,

where , , and are the acceleration, velocity, coordinate and the time-step of a protostar at time t respectively (Swope, et al., 1982). Adaptive time-steps are a way of keeping the workload down whilst improving the accuracy of our numerical integration. In our project, we use an adaptive time-step used in the GADGET-2 code (Springel, 2005), which is defined as,

where is the adaptive time-step, is the maximum time-step that we define and is an accuracy parameter.

**3. Preliminary results**

We use a Sun-Earth-Moon model to verify a working code due to the orbits of the model being well known. To test the adaptive time-steps of our code, we decided to model a very eccentric orbit due to the varying acceleration of the eccentric orbit. The orbits of both models can be seen below.

* Results from Earth moon sun and eccentric orbit, and how it shows a working simulation

**4. Discussion and conclusions**

* Goal for next semester (Discussion)

CHECK YOUR REFERENCES…..

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**[N-body simulations of young protostellar systems]**

**Introduction**

* [Multiplicity of stellar systems]
* [IMF and what it can show and do]

**Outline of my project**

* [The problem we don’t understand]
* [What I’m going to be doing]
* Numerical simulation of multiple protostars inside a potential which arises from filaments
* [How the project will work]
* [results/tests or preliminary results]
* Earth – sun – moon.
* Eccentric orbit
* [goal and strategy for next semester]
* [make it a story whilst being **formal**]